



# A number of conjectures are likely to setup

Zhou Mi <sup>1\*</sup>; Hong Wei Shi <sup>2</sup>

<sup>1</sup> Suqian Economy and Trade Vocational School  
<sup>2</sup> Suqian College

## ABSTRACT

An unresolved conjecture in number theory has great possibility to set up.

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\*Corresponding Author

Zhou Mi

E-mail: [zhoumi19920626@163.com](mailto:zhoumi19920626@163.com)

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## INTRODUCTION:

Have an unresolved conjecture in number theory,

$Q_1=2, q_2=3, q_3=5, Q_4, Q_5, \dots$ , from small to large order write all the prime numbers,

$Q_k=q_1 \cdot q_2 \cdot q_3 \cdot \dots \cdot q_{k+1}$

$Q_1=3, Q_2=7, Q_3=31, Q_4=211, Q_5=2311, Q_6=59 \cdot 509,$

$Q_7=19 \cdot 97 \cdot 277, Q_8=347 \cdot 27953, Q_9=317 \cdot 7037$

$63, Q_{10}=331 \cdot 571 \cdot 34231$

The number five is a prime number, after the number five is a composite number, there is now a question of whether there are infinitely many  $k$  such that  $Q_k$  is a prime number, or the  $Q_k$  number?

Look at a matrix:

In 1934, East India (now Bangladesh) Chandra proposed a square sieve:

The first line is the first of 4, 3 of the tolerance of arithmetic sequence  $4, 7, 10, \dots, 4+3(n-1), \dots$

The second line is the first of 7, 5 of the tolerance of arithmetic sequence  $7, 12, 17, \dots, 7+5(n-1), \dots$

The third line is the first of 10, 7 of the tolerance of arithmetic sequence  $10, 17, 24, \dots, 10+7(n-1), \dots$

The fourth line is the first of 13, 9 of the tolerance of arithmetic sequence  $13, 22, 31, \dots, 13+9(n-1), \dots$

Line  $m$  is the first  $3m+1$ , tolerance of arithmetic sequence  $2m+1, 3m+1, 5m+2, 7m+3, \dots$ , its  $n$  item is  $3m+1+(n-1)(2m+1)=2mn+m+n, \dots$

Write the following array:

First column, second column, third column, fourth column, fifth column... Column n...

First row 47101316...  $4+3(n-1)$ ...  
 Second row 712172227...  $7+5(n-1)$ ...  
 Third row 1017243138...  $10+7(n-1)$ ...  
 Fourth row 1322314049...  $13+9(n-1)$ ...  
 Fifth row 1627384960...  $16+11(n-1)$ ...  
 ... ..

Line  $3m+1$   $5m+2$   $7m+3$   $9m+4$   $11m+5$  m...  $2mn+m+n$ ...  
 ... ..

The secret lies in this square: if a natural number N appears in the table, then  $2N + 1$  is certainly not a prime number; if N does not appear in the table, then  $2N + 1$  is certainly a prime number.

In fact, if  $N=2mn+m+n$ , then  $2N+1=2(2mn+m+n)+1=4mn+2m+2n+1=(2m+1)(2n+1)$ , it is not prime. On

the contrary, the N does not appear in the table, if  $2N+1$  is not a prime number, then  $2N+1$  must be a product of two odd, write  $2N+1=(2m+1)(2n+1)=4mn+2m+2n+1$ ,  $N=2mn+m+n$ , it appears in the table, with the assumption of contradiction. So when N does not appear in the matrix when  $2N+1$  is a prime number.

$Q_k=q_1*q_2*q_3, \dots, *q_{k+1}$ ,  $q_1=2$ , so  $Q_2=2*(q_2*q_3, \dots, Q_k)+1$ , apparently  $q_2*q_3*q_4, \dots, *q_k$

Is the number, so  $q_2*q_3*q_4, *q_k=2N+1$ , N, and the above parties appear in the screen, appearing in square sieve in N has an infinite number if the  $2N+1$  appear or do not appear in the matrix. Then it has an infinite number of the  $Q_k=2*(2N+1)+1$  is prime or composite.

So this conjecture is likely to be established!

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